## Mathematics Instructional Families - Data, Probability and Statistics

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The National Center and State Collaborative (NCSC) is applying the lessons learned from the past decade of research on alternate assessments based on alternate achievement standards (AA-AAS) to develop a multi-state comprehensive assessment system for students with significant cognitive disabilities. The project draws on a strong research base to develop an AA-AAS that is built from the ground up on powerful validity arguments linked to clear learning outcomes and defensible assessment results, to complement the work of the Race to the Top Common State Assessment Program (RTTA) consortia.

Our long-term goal is to ensure that students with significant cognitive disabilities achieve increasingly higher academic outcomes and leave high school ready for postsecondary options. A well-designed summative assessment alone is insufficient to achieve that goal. Thus, NCSC is developing a full system intended to support educators, which includes formative assessment tools and strategies, professional development on appropriate interim uses of data for progress monitoring, and management systems to ease the burdens of administration and documentation. All partners share a commitment to the research-to-practice focus of the project and the development of a comprehensive model of curriculum, instruction, assessment, and supportive professional development. These supports will improve the alignment of the entire system and strengthen the validity of inferences of the system of assessments.

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These materials and documents were developed under the National Center and State Collaborative (NCSC) General Supervision Enhancement Grant and are consistent with its goals and foundations. Any changes to these materials are to be consistent with their intended purpose and use as defined by NCSC.

This document is available in alternative formats upon request.

## nCSC

National Center and State Collaborative
NCSC is a collaborative of 15 states and five organizations.
The states include (shown in blue on map): Arizona, Connecticut, District of Columbia, Florida, Georgia, Indiana, Louisiana, Nevada, Pacific Assessment Consortium (PAC-6) ${ }^{1}$, PennsyIvania, Rhode Island, South Carolina, South Dakota, Tennessee, and Wyoming.

Tier II states are partners in curriculum, instruction, and professional development implementation but are not part of the assessment development work. They are (shown in orange on map): Arkansas, California, Delaware, Idaho, Maine, Maryland, Montana, New Mexico, New York, Oregon, and U.S. Virgin Islands.


[^0]The five partner organizations include: The National Center on Educational Outcomes (NCEO) at the University of Minnesota, The National Center for the Improvement of Educational Assessment (Center for Assessment), The University of North Carolina at Charlotte, The University of Kentucky, and edCount, LLC.


NATIONAL CENTERON EDUCATIONAL OUTCOMES
edCount

150 Pillsbury Drive SE 207 Pattee Hall

# Mathematics Instructional Families -Data, Probability and Statistics 

William Kliche<br>Bill Herrera<br>Shawnee Wakeman<br>Angela Lee<br>Charlene Turner<br>Mariel Zeller<br>NCSC Partner States

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## View of Learning Targets and Families across Grades

## Distribution of Instructional Families: Data Analysis I and II

(K-4) Elementary School Learning Targets $\quad(5-8)$ Middle School Learning Targets
E.DPS-1 Gather and interpret data to answer questions related to a particular/single context.

- Formulate questions, gather data, and build representations;
- Identify and describe variation in data, and describe and compare shapes of distributions and measures of central tendency
E.DPS-2 Conduct simple probability experiments and characterize the outcomes in words, diagrams, or numerically.
M.DPS-1 Design investigations and gather data to answer questions about multiple populations.
- Formulate questions, gather data, and build representations;
- Compare populations by analyzing distributions in terms of variability and measures of central tendency.
M.DPS-2 Conduct probability experiments:
- Generate random samples to characterize variability in estimates and predictions;
- Analyze and build models of the association between two variables.
(9-12) High School Learning Targets H.DPS-1 Design and conduct statistical studies:
- Use appropriate statistical measures for analysis;
- Develop the concepts of statistical inference and statistical significance, especially in relation to probability principles and sampling distributions. H.DPS-2 Use the rules of probability to interpret data, develop explanations, and address real-world problems

| K | Grade 1 | Grade 2 | Grade 3 | Grade 4 | Grade 5 | Grade 6 | Grade 7 | Grade 8 | HS |
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| Formulate Questions/ | Represent and | Draw Conclusions <br> Interpret Data | Develop and Use <br> from Data Collection | Probability Models |
| :--- | :--- | :--- | :--- | :--- | | About a Distribution |
| :--- |

# View of Learning Targets, Families, and CCCs by Grade-band 

## Overview of CCCs: Data Analysis I

## (K-4) Elementary School Learning Targets

E.DPS-1 Gather and interpret data to answer questions related to a particular/single context.

- Formulate questions, gather data, and build representations;
- Identify and describe variation in data, and describe and compare shapes of distributions and measures of central tendency.

| Formulate Questions/ Plan Research | Represent and Interpret Data |  | Draw Conclusions from Data Collection |
| :---: | :---: | :---: | :---: |
| Grades K-1 | Grade 2 | Grade 3 | Grade 4 |
| K.DPS. 1 a 1 Select a question that is answered by collected data K.CC. 5 | 2.DPS.1a5 Select a question about 3 attributes that can be concretely represented 1.MD. 4 | 3.DPS.1f1 Develop questions, make a plan for data collection No CCSS linked | 4.DPS.1f2 Develop questions, make a plan for data collection No CCSS linked |
| 1.DPS. 1 a 2 Select questions that ask about "How many" and represent up to three categories that can be concretely represented <br> 1.MD. 4 | 2.DPS. 1 a6 Identify up to 3 categories resulting from a selected question $\text { 1.MD. } 4$ | 3.DPS. 1 g 1 Collect data, organize into picture or bar graph $\text { 3.MD. } 3$ | 4.DPS. 1 g 3 Collect data, organize in graph (e.g., picture graph, line plot, bar graph) <br> 3.MD. 3 |
| 1.DPS. 1 a3 Identify 2 categories resulting from a selected question 1.MD. 4 | 2.DPS.1a7 Analyze data by sorting into categories established by each question $\text { 2.MD. } 10$ | 3.DPS. 1 g 2 Organize measurement data into a line plot $\text { 3.MD. } 4$ | 4.DPS. 111 (repeated) Select the appropriate statement that describes the data representations based on a given graph (picture, bar, line plots) 3.MD. 3 |
| 1.DPS.1a4 Analyze data by sorting into 2 categories; answer questions about the total number of data points and how many in each category 1.MD. 4 | 2.DPS. 1 a8 Interpret the number of points in each category <br> No CCSS linked <br> 2.DPS.1c2 Organize data by representing categorical data on a pictorial graph or bar graph <br> 2.MD. 10 | 3.DPS. $1 \mathrm{i1}$ Select the appropriate statement that describes the data representations based on a given graph (picture, bar, line plots) <br> 3.MD. 3 | 4.DPS.1j1 Select an appropriate statement that describes the most frequent or the least frequent data point using a line plot, picture graph, or bar graph <br> 4.G. 1 |
| 1.DPS.1c1 Using a picture graph, represent each object/person counted on the graph (1:1 correspondence) for 2 or more categories <br> 1.MD. 4 | 2.DPS.1c3 Organize data by representing continuous data on a line plot $\text { 2.MD. } 9$ | 3.DPS.1k1 Apply results of data to a real-world situation <br> No CCSS linked | 4.DPS.1k2 Apply results of data to a real-world situation <br> 3.MD. 4 |

## (K-4) Elementary School Learning Targets

E.DPS-1 Gather and interpret data to answer questions related to a particular/single context.

- Formulate questions, gather data, and build representations;
- Identify and describe variation in data, and describe and compare shapes of distributions and measures of central tendency.
Formulate Questions/ Plan Research $\quad$ Represent and Interpret Data $\quad$ Draw Conclusions from Data Collection

| Grades K-1 | Grade 2 | Grade 3 | Grade 4 |
| :---: | :---: | :---: | :---: |
| 1.DPS.1d1 Interpret a picture graph to answer questions about how many in each category $\text { 1.MD. } 4$ | 2.DPS.1d2 Identify the value of each category represented on picture graph and bar graph or each point on a line plot <br> 2.MD. 9 <br> 2.MD. 10 |  |  |
| 1.DPS.1e1 Compare the values of the 2 categories of data in terms of more or less <br> 1.MD. 4 | 2.DPS.1e2 Compare the information shown in a bar graph or picture graph with up to 4 categories. Solve simple comparisons of how many more or how many less $\text { 2.MD. } 10$ |  |  |

## Overview of CCCs: Data Analysis I

## (5-8) Middle School Learning Targets

M.DPS-1 Design investigations and gather data to answer questions about multiple populations.

- Formulate questions, gather data, and build representations;
- Compare populations by analyzing distributions in terms of variability and measures of central tendency.

| Formulate Questions/ Plan Research | Represent and Interpret Data | Draw Conclusions from Data Collection |  |
| :--- | :--- | :--- | :--- | :--- |
| Grade 5 | Grade 6 | Grade 7 | Grade 8 |

## (5-8) Middle School Learning Targets

M.DPS-1 Design investigations and gather data to answer questions about multiple populations.

- Formulate questions, gather data, and build representations;
- Compare populations by analyzing distributions in terms of variability and measures of central tendency.



## Overview of CCCs: Data Analysis II

## (5-8) Middle School Learning Targets

## M.DPS-2 Conduct probability experiments:

- Generate random samples to characterize variability in estimates and predictions;
- Analyze and build models of the association between two variables.

| Develop and Use Probability Models | Draw Inferences About a Distribution |
| :---: | :---: |
| Grade 7 | Grade 8 |
| 7.DPS.2a1 Conduct simple probability experiments No CCSS link | 8.DPS.2e4 Determine the theoretical probability of multistage probability experiments (2 coins, 2 dice) <br> 7.SP. 8 |
| 7.DPS.2d1 Describe the probability of events as being certain or impossible, likely, less likely or equally likely 7.SP. 5 |  |
| 7.DPS.2d2 State the theoretical probability of events occurring in terms of ratios (words, percentages, decimals) <br> 7.SP. 5 | 8.DPS.2e5 Collect data from multistage probability experiments (2 coins, 2 dice) <br> 7.SP. 8 |
| 7.DPS.2b1 Identify sample space for a single event (coin, spinner, die) No CCSS linked | 8.DPS.2e6 Compare actual results of multistage experiment with theoretical probabilities $\text { 7.SP. } 8$ |
| 7.DPS.2d3 Using a tree diagram, represent all possible outcomes of a situation, with up to 3 compound events with 2 or 3 possibilities per category (selecting the color of shirt, pant, type of shoes) 7.SP. 6 | 8.DPS. 2 g 1 Distinguish between a linear and non-linear association when analyzing bivariate data on a scatter plot 8.SP. 2 |
| 7.DPS.2d4 Make a prediction regarding the probability of an event occurring; conduct simple probability experiments $\text { 7.SP. } 6$ |  |
| 7.DPS.2e1 Determine the theoretical probability of multistage probability experiments (2 coins, 2 dice) 7.SP. 8 |  |
| 7.DPS. 2 e2 Collect data from multistage probability experiments (2 coins, 2 dice) <br> 7.SP. 8 |  |
| 7.DPS.2d5 Compare actual results of simple experiment with theoretical probabilities <br> 7.SP. 7 |  |

## (5-8) Middle School Learning Targets

## M.DPS-2 Conduct probability experiments

- Generate random samples to characterize variability in estimates and predictions;
- Analyze and build models of the association between two variables.

| Develop and Use Probability Models | Draw Inferences About a Distribution |
| :--- | :--- |
| Grade 7 | Grade 8 |
| 7.DPS.2e3 Compare actual results of multistage experiment with theoretical <br> probabilities <br> $7 . S P .8$ |  |

## Overview of CCCs: Data Analysis I

| (9-12) High School Learning Targets |  |  |
| :---: | :---: | :---: |
| H.DPS-1 Design and conduct statistical studies: <br> - Use appropriate statistical measures for analysis; <br> - Develop the concepts of statistical inference and statistical significance, especially in relation to probability principles and sampling distributions. |  |  |
| Formulate Questions/ Plan Research | Represent and Interpret Data | Draw Conclusions from Data Collection |
| HS |  |  |
| H.DPS. 1 a1 Design study using categorical and continuous data, including creating a question, identifying a sample, and making a plan for data collection S.ID. 4 <br> S.ID. 5 |  |  |
| H.DPS. 1 b1 Complete a graph given the data, using dot plots, histograms, or box plots S.ID. 1 |  |  |
| H.DPS.1c1 Use descriptive stats; range, median, mode, mean, outliers/gaps to describe the data set S.ID. 4 <br> S.ID. 5 |  |  |
| H.DPS. 1 d1 Represent data on a scatter plot to describe and predict S.ID. 6 |  |  |
| H.DPS. 1 c 2 Compare means, median, and range of 2 sets of data S.ID. 2 |  |  |
| H.DPS. 1 d 2 Select an appropriate statement that describes the relationship between variables S.ID. 6 |  |  |
| H.DPS. 1 d3 Make or select an appropriate statement(s) about findings S.IC. 6 |  |  |
| H.DPS. 1 d4 Apply the results of the data to a real-world situation S.IC. 6 |  |  |

## Overview of CCCs: Data Analysis II

## (9-12) High School Learning Targets

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H.DPS-1 Design and conduct statistical studies:
- Use appropriate statistical measures for analysis;
- Develop the concepts of statistical inference and statistical significance, especially in relation to probability principles and sampling distributions.
H.DPS-2 Use the rules of probability to interpret data, develop explanations, and address real-world problems
Develop and Use Probability Models 
HS
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H.DSP.2b1 Identify and describe the degree to which something is rated "good" or "bad"/desirable or undesirable based on numerical information
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H.DSP.2b1 Identify and describe the degree to which something is rated "good" or "bad"/desirable or undesirable based on numerical information
S.MD.7
S.MD.7
H.DPS.2c1 Determine the theoretical probability of multistage probability experiments
S.MD.3
H.DPS.2c2 Collect data from multistage probability experiments
S.MD. }
H.DPS.1c3 Determine what inferences can be made from statistics
S.IC. }
H.DPS.2c3 Compare actual results of multistage experiment with theoretical probabilities
S.MD. }
H.DSP.2d1 Select or make an appropriate statement based on a two-way frequency table
S.CP. }
H.DSP.2e1 Select or make an appropriate statement based on real-world examples of conditional probability
S.CP.5

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\section*{View by Instructional Families and CCSS Domains}

\section*{Instructional Families: Data Analysis I}
\begin{tabular}{|c|c|c|}
\hline CCSS Domain: Counting and Cardinality; Measurement and Data & CCSS Domain: Measurement and Data; Statistics and Probability & CCSS Domain: Measurement and Data; Statistics and Probability; Interpreting Categorical and Quantitative Data; Making Inferences and Justifying Conclusions \\
\hline Formulate Questions/Plan Research & Represent and Interpret Data & Draw Conclusions from Data Collection \\
\hline K.DPS.1a1 Select a question that is answered by collected data
\[
\text { K.CC. } 5
\] & \begin{tabular}{l}
1.DPS. 1 a4 Analyze data by sorting into 2 categories; answer questions about the total number of data points and how many in each category \\
1.MD. 4
\end{tabular} & \begin{tabular}{l}
1.DPS.1e1 Compare the values of the 2 categories of data in terms of more or less \\
1.MD. 4
\end{tabular} \\
\hline 1.DPS. 1 a2 Select questions that ask about "How many" and represent up to three categories that can be concretely represented 1.MD. 4 & 1.DPS.1c1 Using a picture graph, represent each object/person counted on the graph (1:1 correspondence) for 2 or more categories 1.MD. 4 & \begin{tabular}{l}
2.DPS. 1 e2 Compare the information shown in a bar graph or picture graph with up to 4 categories. Solve simple comparisons of how many more or how many less \\
2.MD. 10
\end{tabular} \\
\hline \begin{tabular}{l}
1.DPS.1a3 Identify 2 categories resulting from a selected question \\
1.MD. 4
\end{tabular} & 1.DPS.1d1 Interpret a picture graph to answer questions about how many in each category 1.MD. 4 & \begin{tabular}{l}
3.DPS. 1 k 1 Apply results of data to a real-world situation \\
No CCSS linked
\end{tabular} \\
\hline \begin{tabular}{l}
2.DPS. 1 a5 Select a question about 3 attributes that can be concretely represented \\
1.MD. 4
\end{tabular} & \begin{tabular}{l}
2.DPS. 1 a 7 Analyze data by sorting into categories established by each question \\
2.MD. 10
\end{tabular} & 4.DPS.1k2 Apply results of data to a real-world situation
\[
\text { 3.MD. } 4
\] \\
\hline \begin{tabular}{l}
2.DPS. 1 a6 Identify up to 3 categories resulting from a selected question \\
1.MD. 4
\end{tabular} & \begin{tabular}{l}
2.DPS. 1 a 8 Interpret the number of points in each category \\
No CCSS linked
\end{tabular} & 5.DPS.1e1 Use measures of central tendency to interpret data including overall patterns in the data 6.SP. 3 \\
\hline \begin{tabular}{l}
3.DPS.1f1 Develop questions, make a plan for data collection \\
No CCSS linked
\end{tabular} & 2.DPS.1c2 Organize data by representing categorical data on a pictorial graph or bar graph 2.MD. 10 & 6.DPS. 1 d 5 Explain or identify what the mean represents in a set of data 6.SP. 3 \\
\hline \begin{tabular}{l}
4.DPS. 1 f2 Develop questions, make a plan for data collection \\
No CCSS linked
\end{tabular} & 2.DPS. 1 c3 Organize data by representing continuous data on a line plot 2.MD. 9 & 6.DPS.1d6 Explain or identify what the mode represents in a set of data 6.SP. 2 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline CCSS Domain: Counting and Cardinality; Measurement and Data & CCSS Domain: Measurement and Data; Statistics and Probability & CCSS Domain: Measurement and Data; Statistics and Probability; Interpreting Categorical and Quantitative Data; Making Inferences and Justifying Conclusions \\
\hline Formulate Questions/Plan Research & Represent and Interpret Data & Draw Conclusions from Data Collection \\
\hline 6.DPS. 1 a2 Identify statistical questions and make a plan for data collection
\[
\text { 6.SP. } 1
\] & 2.DPS.1d2 Identify the value of each category represented on picture graph and bar graph or each point on a line plot
\[
\begin{aligned}
& \text { 2.MD. } 9 \\
& \text { 2.MD. } 10
\end{aligned}
\] & 6.DPS.1d7 Explain or identify what the median represents in a set of data 6.SP. 5 \\
\hline 7.DPS.1b1 Determine sample size to answer a given question 7.SP. 1 & \begin{tabular}{l}
3.DPS. 1 g 1 Collect data, organize into picture or bar graph \\
3.MD. 3
\end{tabular} & 6.DPS. 1 e2 Use measures of central tendency to interpret data including overall patterns in the data 6.SP. 5 \\
\hline 8.DPS.1f1 Formulate a research question to study No CCSS linked & \begin{tabular}{l}
3.DPS. 1 g2 Organize measurement data into a line plot \\
3.MD. 4
\end{tabular} & 7.DPS. 111 Make or select a statement to compare the distribution of 2 data sets 7.SP. 3 \\
\hline 8.DPS. 1 f2 Identify two variables to study in a given a research question No CCSS linked & \begin{tabular}{l}
3.DPS. 111 Select the appropriate statement that describes the data representations based on a given graph (picture, bar, line plots) \\
3.MD. 3
\end{tabular} & 7.DPS. 1 k 1 Analyze graphs to determine or select appropriate comparative inferences about two samples or populations 7.SP. 4 \\
\hline \begin{tabular}{l}
H.DPS.1a1 Design study using categorical and continuous data, including creating a question, identifying a sample, and making a plan for data collection \\
S.ID. 4 \\
S.ID. 5
\end{tabular} & 4.DPS. 1 g3 Collect data, organize in graph (e.g., picture graph, line plot, bar graph) 3.MD. 3 & 8.DPS. 1 j 2 Make or select an appropriate statements based upon two unequal data sets using measure of central tendency and shape
\[
\text { 7.SP. } 4
\] \\
\hline \multirow[t]{2}{*}{} & 4.DPS. 111 (repeated) Select the appropriate statement that describes the data representations based on a given graph (picture, bar, line plots) 3.MD. 3 & \begin{tabular}{l}
8.DPS.1k2 Analyze displays of bivariate data to develop or select appropriate claims about those data \\
8.SP. 4
\end{tabular} \\
\hline & 4.DPS. 1 j 1 Select an appropriate statement that describes the most frequent or the least frequent data point using a line plot, picture graph, or bar graph
\[
\text { 4.G. } 1
\] & H.DPS. 1 c 2 Compare means, median, and range of 2 sets of data
\[
\text { S.ID. } 2
\] \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline \(\begin{array}{l}\text { CCSS Domain: Counting and } \\
\text { Cardinality; Measurement and Data }\end{array}\) & \(\begin{array}{l}\text { CCSS Domain: Measurement and Data; } \\
\text { Statistics and Probability }\end{array}\) & \(\begin{array}{l}\text { CCSS Domain: Measurement and Data; } \\
\text { Statistics and Probability; Interpreting } \\
\text { Categorical and Quantitative Data; } \\
\text { Making Inferences and Justifying } \\
\text { Conclusions }\end{array}\) \\
\hline Formulate Questions/Plan Research & \multicolumn{1}{|c|}{ Represent and Interpret Data } & Draw Conclusions from Data Collection
\end{tabular}\(\}\)
\begin{tabular}{|c|c|c|}
\hline CCSS Domain: Counting and Cardinality; Measurement and Data & CCSS Domain: Measurement and Data; Statistics and Probability & CCSS Domain: Measurement and Data; Statistics and Probability; Interpreting Categorical and Quantitative Data; Making Inferences and Justifying Conclusions \\
\hline Formulate Questions/Plan Research & Represent and Interpret Data & Draw Conclusions from Data Collection \\
\hline \multirow[t]{8}{*}{} & 8.DPS. \(1 \mathrm{f3}\) Construct a two-way table summarizing data on two categorical variables collected from the same subjects; identify possible association between the two variables
\[
\text { 8.SP. } 4
\] & \\
\hline & 8.DPS.1g2 Graph data using line graphs, histograms, or box plots 8.SP. 1 & \\
\hline & 8.DPS.1h1 Graph bivariate data using scatter plots and identify possible associations between the variables 8.SP. 1 & \\
\hline & 8.DPS. 1 i3 Using box plots and scatter plots, identify data points that appear to be outliers 8.SP. 1 & \\
\hline & 8.DPS. 1 i 4 Identify outliers, range, mean, median, and mode
6.SP.5c & \\
\hline & H.DPS.1b1 Complete a graph given the data, using dot plots, histograms, or box plots S.ID. 1 & \\
\hline & H.DPS.1c1 Use descriptive stats; range, median, mode, mean, outliers/gaps to describe the data set S.ID. 4
\[
\text { S.ID. } 5
\] & \\
\hline & H.DPS.1d1 Represent data on a scatter plot to describe and predict
\[
\text { S.ID. } 6
\] & \\
\hline
\end{tabular}

\section*{Instructional Families: Data Analysis II}
\begin{tabular}{|c|c|}
\hline CCSS Domain: Statistics and Probability; Using Probability to Make Decisions & CCSS Domain: Statistics and Probability; Using Probability to Make Decisions; Conditional Probability and the Rules of Probability \\
\hline Develop and Use Probability Models & Draw Inferences about a Distribution \\
\hline 7.DPS.2a1 Conduct simple probability experiments No CCSS linked & \begin{tabular}{l}
7.DPS.2d5 Compare actual results of simple experiment with theoretical probabilities \\
7.SP. 7
\end{tabular} \\
\hline \begin{tabular}{l}
7.DPS.2d1 Describe the probability of events as being certain or impossible, likely, less likely or equally likely \\
7.SP. 5
\end{tabular} & \begin{tabular}{l}
7.DPS.2e3 Compare actual results of multistage experiment with theoretical probabilities \\
7.SP. 8
\end{tabular} \\
\hline \begin{tabular}{l}
7.DPS.2d2 State the theoretical probability of events occurring in terms of ratios (words, percentages, decimals) \\
7.SP. 5
\end{tabular} & \begin{tabular}{l}
8.DPS.2e6 Compare actual results of multistage experiment with theoretical probabilities \\
7.SP. 8
\end{tabular} \\
\hline 7.DPS.2b1 Identify sample space for a single event (coin, spinner, die) No CCSS linked & 8.DPS. 2 g 1 Distinguish between a linear and non-linear association when analyzing bivariate data on a scatter plot 8.SP. 2 \\
\hline 7.DPS.2d3 Using a tree diagram, represent all possible outcomes of a situation, with up to 3 compound events with 2 or 3 possibilities per category (selecting the color of shirt, pant, type of shoes) 7.SP. 6 & H.DPS. 1 c3 Determine what inferences can be made from statistics S.IC. 1 \\
\hline 7.DPS.2d4 Make a prediction regarding the probability of an event occurring; conduct simple probability experiments
\[
\text { 7.SP. } 6
\] & \begin{tabular}{l}
H.DPS.2c3 Compare actual results of multistage experiment with theoretical probabilities \\
S.MD. 3
\end{tabular} \\
\hline 7.DPS.2e1 Determine the theoretical probability of multistage probability experiments (2 coins, 2 dice) 7.SP. 8 & H.DSP.2d1 Select or make an appropriate statement based on a two-way frequency table S.CP. 4 \\
\hline 7.DPS.2e2 Collect data from multistage probability experiments (2 coins, 2 dice)
\[
\text { 7.SP. } 8
\] & H.DSP.2e1 Select or make an appropriate statement based on real-world examples of conditional probability
\[
\text { S.CP. } 5
\] \\
\hline 8.DPS.2e4 Determine the theoretical probability of multistage probability experiments (2 coins, 2 dice) 7.SP. 8 & \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
CCSS Domain: Statistics and Probability; Using Probability to \\
Make Decisions
\end{tabular} & \begin{tabular}{l} 
CCSS Domain: Statistics and Probability; Using Probability to \\
Make Decisions; Conditional Probability and the Rules of \\
Probability
\end{tabular} \\
\hline \multicolumn{1}{|c|}{ Develop and Use Probability Models } & Draw Inferences about a Distribution \\
\hline \begin{tabular}{l} 
8.DPS.2e5 Collect data from multistage probability experiments (2 coins, 2 \\
dice)
\end{tabular} \\
7.SP.8
\end{tabular}```


[^0]:    ${ }^{1}$ The Pacific Assessment Consortium (including the entities of American Samoa, Commonwealth of the Northern Mariana Islands, Federated States of Micronesia, Guam, Republic of Palau, and Republic of the Marshall Islands) partner with NCSC as one state, led by the University of Guam Center for Excellence in Developmental Disabilities Education, Research, and Service (CEDDERS).

