# Solving two-step equations with fractions and decimals 

National Center and State Collaborative

## Two methods for solving two step equations

## Method 1: isolate the variable

$$
\begin{aligned}
& \frac{r+7}{4}=5 \\
& \frac{r}{4}+\frac{7}{4}=5 \quad \longleftarrow \\
& \begin{array}{l}
\text { Step 1: rewrite to } \\
\text { sum of two } \\
\text { fractions }
\end{array}
\end{aligned}
$$

$\frac{r}{4}+\frac{7}{4}-\frac{7}{4}=5-\frac{7}{4} \longleftarrow \quad \begin{aligned} & \text { Step 2: subtract } \\ & \text { both sides by 7/4 }\end{aligned}$
(4) $\frac{r}{4}=\frac{13}{4}(4) \longleftarrow$ Step 3: multiply both sides by 4
$r=13$

## Method 2: Multiply both sides by the denominator

$$
\begin{array}{ll}
\frac{r+7}{4}=5 & \\
\text { (4) } \frac{r+7}{4}=5(4) \longleftarrow & \text { Step 1: multiply } \\
\text { both sides by } 4
\end{array}
$$

$r+7=20$
$r=13$

## Solving two step word problem

The Smith family spent $\$ 52.00$ on concert tickets. This cost included a $\$ 3.25$ service fee for buying them online and the original cost of the ticket was $\$ 9.75$ each. How many tickets did the Smiths buy?

$$
\begin{array}{cc}
\text { Total cost }=\quad \text { tickets }+\quad \text { service fee } \\
52.00=9.75 t+3.25 & \\
52.00-3.25=9.75 t+3.25-3.25 \longleftarrow & \begin{array}{l}
\text { Step 1: subtract } 3.25 \text { from } \\
\text { each side }
\end{array} \\
\frac{48.75}{9.75}=\frac{9.75 t}{9.75} \longleftarrow & \begin{array}{l}
\text { Step 2: divide both sides } \\
\text { by } 9.75
\end{array} \\
5=\mathrm{t} &
\end{array}
$$

## Ideas for application

- Create personally-relevant word problems
- Example: Your car broke down, labor to fix it cost $\$ 40$ per hour plus $\$ 430$ for the parts. The total cost is $\$ 630$. How many hours of labor did it take?
- Color code parts of the equation as shown in the examples in this PowerPoint
- Check answers by plugging the answer into the original equation to make sure both sides are equal


## Making connections

- Multiplying and dividing decimals address the following $6^{\text {th }}$ and $8^{\text {th }}$ grade Core Content Connectors
- 6.NO.2c3 Solve one step addition, subtraction, multiplication, or division problems with fractions or decimals
- 8.NO.2i4 Solve two step addition, subtraction, multiplication, and division problems with fractions, decimals, or positive/negative numbers

